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QUANTIFICATION OVER LINES

Let \mathcal{A} be a first-order model for the language L (with universum A) and q be a family of subsets of A . $\langle \mathcal{A}, q \rangle$ is called a *geometric model* iff the family q satisfies.

- (i) every member of q is infinite,
- (ii) the intersection of any two different sets from q contains at most one element,
- (iii) for any different points $a, b \in A$ there is some $X \in q$ which contains a and b .

Now the language L is extended by the extra quantifier Q which has the intended meaning “there is some $U \in q$ such that for all $x \in U \dots$ ”. We consider the logic of all sentences of $L(Q)$ valid in all geometric models. There is a set of axioms for this logic for which we can prove the completeness theorem.

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